



Institute of Mathematics

Winter semester:

Module I

Analysis	
Differential Equations	20 ECTS
Geometry	20 EC 15
Linear Algebra	

Summer semester:

Module I

Algebra	
Differential Geometry	20 ECTS
Numerical Analysis	20 EC 15
Topology	





Course title	Analysis						
Semester (winter/summer)	winter	ECTS	5				
Lecturer(s)	Dr Paweł Wójcik						
Department	Mathematics						

Course objectives (learning outcomes)

Introduction to the theory and methods of analysis in one or two real variable. Introduction to the theory of measure.

Knowledge	There are no prerequisites.
Skills	There are no prerequisites.
Courses completed	There are no prerequisites.

Course organization										
Form of classes	W (Lecture)	Group type								
Form of classes		A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)			
Contact hours			15							





Discussions and exercises including computer usage (e.g. Maxima).

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria Students have to write one or two essays.

Comments

Course content (topic list)

- 1. Real numbers and theirs subset.
- 2. Continuous functions.
- 3. Derivatives of functions with one variable.
- 4. Minimum, maximum and monotonicity of functions.
- 5. The Riemann integral.
- 6. Metric spaces (open, closed and compact subset).
- 7. Uniform convergence.
- 8. Derivatives of functions with two or three variables.
- 9. Minimum and maximum of functions with two variables
- 10. Lebesgue measure.and Lebesgue integral

Compulsory reading

Tao, T.: Analysis I, Hindustan Book Agency https://lms.umb.sk/pluginfile.php/111477/mod_page/content/5/TerenceTao_Analysis.I.Third.Edition.pdf

Recommended reading Rudin, W.: Principles of mathematical analysis, McGraw-Hill Science 1976





Course title	Differential Equations						
Semester (winter/summer)	winter	ECTS	5				
Lecturer(s)	Dr hab. Leszek Gasiński, prof. UP						
Department	Mathematics						

Course objectives (learning outcomes)

Introduction to the theory and methods of differential equations

Knowledge	Differential calculus of functions of one and several variables. Integral calculus. Algebra of matrices and determinants.	
Skills	Calculation of derivatives of functions of one and several variables. Calculation of integrals.	
Courses completed	Mathematical Analysis. Linear Algebra.	

Course organization										
Form of classes	W (Lecture)	Group type								
Form of classes	w (Lecture)	A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)			
Contact hours			15							





Discussions and exercises.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria Students have to write one or two essays.

Comments

Course content (topic list)

- 1. Origin of Differential Equations
- 2. Differential Equations of First Order
- 3. Linear Differential Equations of Second Order
- 4. Linear Partial Differential Equations of First Order

Compulsory reading

- 1. W. Walter, Ordinary Differential Equations. Graduate Texts in Mathematics: Springer, 1998.
- 2. F. Ayres, JR., *Theory and Problems of Differential Equations*: Schaum's Outline Series, McGraw-Hill Book Company, New York, St. Louis, San Francisco, Toronto, Sydney, 1952.

Recommended reading

- 1. B. Spain, *Ordinary Differential Equations*: Van Nostrand Reinhold Company, London, New York, Toronto, Melbourne, 1969.
- 2. Shepley L. Ross, *Differential Equations*: Blaisdell Publishing Company, New York, Toronto, London, 1964.





Course title	Geometry						
Semester (winter/summer)	winter	ECTS	5				
Lecturer(s)	Prof. dr hab. Tomasz Szemberg Dr hab. Justyna Szpond						
Department	Mathematics						

Course objectives (learning outcomes)

Introduction to the theory and methods of elementary geometry.

Knowledge	There are no prerequisites.
Skills	Plotting points and figures in Cartesian coordinates.
Courses completed	There are no prerequisites.

Course organization											
Form of classes	W (Lecture)			Gro							
	W (Lecture)	A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)				
Contact hours			15			15					





Discussions and exercises.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria	Students have to write an essay.

Comments

Course content (topic list)

- 1. Triangles.
- 2. Isometries in the plane.
- 3. Similarities.
- 4. Circles and spheres.
- 5. Coordinates.
- 6. Complex numbers.

Compulsory reading

Coxeter, H.S.M.: Introduction to geometry, Wiley 1969

Recommended reading

Coxeter, H.S.M., Greizer, S.M.: Geometry revisited, The Mathematical Association of America 1967





Course title	Linear Algebra										
Semester (winter/summer)	winter	ECTS	5								
Lecturer(s)	Dr Karol Gryszka										
Department	Institute of Mathematics										

Course objectives (learning outcomes)

The aim of the course is to familiarize students with the main concepts and terminology of linear algebra. Emphasis is given to systems of linear equations, matrices, and vector spaces, determinants, eigenvalues, orthogonality and symmetric matrices.

Knowledge	There are no prerequisites
Skills	There are no prerequisites
Courses completed	There are no prerequisites

Course organization											
Form of classes	W (Lecture)	Group type									
	w (Lecture)	A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)				
Contact hours			15								





Reading course, tutorials.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
							×		×			

Assessment criteria	Active participation in tutorials.
Assessment enteria	Submitted written assignment.

Comments

Course content (topic list)

- 1. Matrices, matrix operations and inverses.
- 2. Systems of linear equations.
- 3. Vector spaces definition and examples.
- 4. Linear independence, basis and dimension.
- 5. Linear maps.
- 6. Range space and null space.
- 7. Representing linear maps with matrices.
- 8. Determinants properties of determinants, the permutation expansion.
- 9. Eigenvalues and eigenvectors, invariant subspaces.
- 10. Diagonalizability.
- 11. Inner product, orthonormal bases.
- 12. Orthogonal projection into a line, geometric view of orthogonal projections.
- 13. Gram-Schmidt orthogonalization.
- 14. Symmetric matrices.

Compulsory reading

1. Sheldon Axler - Linear Algebra Done Right, Undergraduate Texts in Mathematics, Springer 2. Jim Hefferon - Linear Algebra (available free at: http://joshua.smcvt.edu/linearalgebra)

Recommended reading

David C. Lay - Linear Algebra and Its Applications, Pearson









Course title	Algebra										
Semester (winter/summer)	summer	ECTS	5								
Lecturer(s)	dr hab. Katarzyna Słomczyńska, prof. UP dr hab. Janusz Gwoździewicz, prof. UP										
Department	Mathematics										

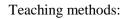
Course objectives (learning outcomes)

Introduction to the theory of groups, rings and fields.

Knowledge	Complex numbers, foundations of the linear algebra (matrix theory).
Skills	Proficiency in numbers and matrix computations.
Courses completed	Introduction to Logic and Set Theory. Linear Algebra.

Course organization											
Form of classes	W (Lecture)			Gro	oup type						
	w (Leeture)	A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)				
Contact hours			15								







Discussions and exercises.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria	Active participation in tutorials.
Assessment criteria	Students have to write one or two essays.

Comments

Course content (topic list)

1. Group theory: basic axioms and examples, groups of permutations, subgroups, cyclic groups, quotient groups and homomorphisms, Lagrange's Theorem, Isomorphism Theorems, finite abelian groups, group actions on sets, solvable groups.

2. Ring theory: basic definitions and examples, ideals and quotient rings, ring homomorphisms, Chinese Remainder Theorem, prime and maximal ideals, polynomial rings over fields.

3. Field theory: characteristic of a field, field of fractions, field extensions, algebraic and transcendental numbers, finite fields.

Compulsory reading

T. W. Hungerford, Algebra, Springer 1996

Recommended reading

http://www.jmilne.org/math/CourseNotes/GT.pdf https://www2.bc.edu/mark-reeder/Groups.pdf http://www.jmilne.org/math/CourseNotes/FT.pdf http://www1.spms.ntu.edu.sg/~frederique/chap2.pdf





Course title	Differential Geometry					
Semester (winter/summer)	summer	ECTS	5			
Lecturer(s)	Dr hab. Justyna Szpond Prof. dr hab. Tomasz Szemberg					
Department	Mathematics					

Course objectives (learning outcomes)

Introduction to the theory of curves and surfaces, and methods of differential geometry.

Knowledge	Elements of algebra and vector analysis. Vector spaces, linear and multilinear mappings. Calculus of functions of several variables.
Skills	Calculating of derivatives of functions of several variables.
Courses completed	Introduction to Logic and Set Theory Mathematical Analysis Linear Algebra Geometry

Course organization									
Form of classes	W (Lecture)	Group type							
Form of classes	W (Lecture)	A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)		
Contact hours			15			15			





Discussions and exercises.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria Students have to write one or two essays.

Comments

Course content (topic list)

1. Curves

- 1. Examples, Arclength Paramatrization
- 2. Local Theory: Frenet Frame
- 3. Some Global Results

2. Surfaces

- 1. Parametrized Surfaces and the First Fundamental Form
- 2. The Gauss Map and the Second Fundamental Form
- 3. The Codazzi and Gauss Equations and the Fundamental Theorem of Surface Theory

Compulsory reading

T. Shifrin, *Differential Geometry*: A First Course on Curves and Surfaces available free at: *www.math.uga.edu/~shifrin/ShifrinDiffGeo.pdf*

Recommended reading Michael David Spivak, A Comprehensive Introduction to Differential Geometry. Publish or Perish 2005





Course title	Numerical Analysis					
Semester (winter/summer)	summer	ECTS	5			
Lecturer(s)	dr Zbigniew Leśniak					
Department	Institute of Mathematics					

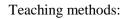
Course objectives (learning outcomes)

The aim of the course is to familiarize students with the basic concepts of analysis and implementations of algorithms for solving numerically the problems of continuous mathematics (as opposed to symbolic manipulations). Topics covered include: fundamental principles of digital computing and the implications for algorithm accuracy and stability. Emphasis is given to understanding the behaviour of numerical methods for solving linear algebra problems.

Knowledge	Familiar with basics of linear algebra and real analysis.
Skills	Familiar with basics of Visual C#, C++ or Java.
Courses completed	There are no prerequisites.

Course organization									
Form of classes	W (Lecture)	Group type							
Form of classes		A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)		
Contact hours			15						







Reading course, tutorials.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
							×		×			

Assessment criteria	Active participation in tutorials.
Assessment criteria	Submitted written assignment.

Comments

Course content (topic list)

- 11. Floating-point representation of numbers.
- 12. Finite precision arithmetic, the limits on the accuracy.
- 13. Round-off errors, truncation and discretization error.
- 14. Sensitivity of the solution of a problem to small changes in the data, ill-conditioned problems.
- 15. Backward error analysis, numerical stability of algorithms.
- 16. Interval arithmetic.
- 17. Numerically stable algorithms for computing values of functions.
- 18. Numerically stable algorithms for solving linear systems of equations.

Compulsory reading

- 1. Ward Cheney, David Kincaid Numerical Mathematics and Computing, Thompson Brooks/Cole
- Germund Dahlquist, Åke Björck Numerical Methods in Scientific Computing, Volume 1, SIAM (working copy available for students enrolled in specific courses at: http://cristiancastrop.files.wordpress.com/2010/09/dahlquist-bjorck-vol-1.pdf)

Recommended reading

Åke Björck - Numerical Methods in Scientific Computing, Volume 2, SIAM





Course title	Topology					
Semester (winter/summer)	summer	ECTS	5			
Lecturer(s)	Dr hab. Jacek Chmieliński, prof. UP					
Department	Institute of Mathematics					

Course objectives (learning outcomes)

The aim of the course is to familiarize students with metric and topological spaces and their basic properties such as completeness, compactness and connectedness, to the extent enabling usage these concepts in other courses (e.g. in functional analysis).

Knowledge	Familiar with the elementary set theory. Familiar with basics of calculus (the set of reals as a metric space, properties of functions, limits, continuity, etc.)
Skills	Able to compute the limit of a sequence of real numbers, verify continuity of a mapping.
Courses completed	Mathematical Analysis 1 (Calculus 1)

Course organization										
Form of classes	W (Lecture)	Group type								
		A (large group)	K (small group)	L (Lab)	S (Seminar)	P (Project)	E (Exam)			
Contact hours			15							





Reading course, tutorials.

Assessment methods:

E – learning	Didactic games	Classes in schools	Field classes	Laboratory tasks	Individual project	Group project	Discussion participation	Student's presentation	Written assignment	Oral exam	Written exam	Other
									×			

Assessment criteria	Active participation in tutorials.
	Submitted essay.

Comments

Course content (topic list)

- 1. Metric spaces
- 2. Topological spaces basic properties of sets
- 3. Basis, axioms of countability
- 4. Continuity and homeomorphisms, topological invariants
- 5. Axioms of separability
- 6. Completeness, compactness and connectedness

Compulsory reading

1. K. Kuratowski, *Introduction To Set Theory and Topology*, Part II, Pergamon Press & PWN, 1962, 1972. 2. M.A. Armstrong, *Basic Topology*, Undergraduate Texts in Mathematics. Springer-Verlag, New York-Berlin, 1983.

Recommended reading - courses available in the Internet e.g.:

- 1. T.W. Koerner, Metric and Topological Spaces, https://www.dpmms.cam.ac.uk/~twk/Top.pdf
- 2. A. Hatcher, Notes on Introductory Point-Set Topology, https://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
- 3. S.A. Morris, Topology without tears (English and various translations), http://www.topologywithouttears.net/